



SUMMER– 2019 EXAMINATION

Subject Name: Applied Mathematics

Model Answer

Subject Code:

22206

**Important Instructions to Examiners:**

- 1) The answers should be examined by key words and not as word-to-word as given in the model answer scheme.
- 2) The model answer and the answer written by candidate may vary but the examiner may try to assess the understanding level of the candidate.
- 3) The language errors such as grammatical, spelling errors should not be given more Importance (Not applicable for subject English and Communication Skills).
- 4) While assessing figures, examiner may give credit for principal components indicated in the figure. The figures drawn by candidate and model answer may vary. The examiner may give credit for any equivalent figure drawn.
- 5) Credits may be given step wise for numerical problems. In some cases, the assumed constant values may vary and there may be some difference in the candidate's answers and model answer.
- 6) In case of some questions credit may be given by judgement on part of examiner of relevant answer based on candidate's understanding.
- 7) For programming language papers, credit may be given to any other program based on equivalent concept.

Q. No.	Sub Q.N.	Answers	Marking Scheme
1.		<b>Attempt any <u>FIVE</u> of the following:</b>	<b>10</b>
	a)	State whether the function is even or odd, If $f(x) = 3x^4 - 2x^2 + \cos x$	<b>02</b>
	Ans	$f(x) = 3x^4 - 2x^2 + \cos x$ $\therefore f(-x) = 3(-x)^4 - 2(-x)^2 + \cos(-x)$ $\therefore f(-x) = 3x^4 - 2x^2 + \cos x$ $\therefore f(-x) = f(x)$ $\therefore$ function is an even function	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
	b)	If $f(x) = x^2 + 6x + 10$ find $f(2) + f(-2)$	<b>02</b>
	Ans	$f(2) = (2)^2 + 6(2) + 10 = 26$ $f(-2) = (-2)^2 + 6(-2) + 10 = 2$ $\therefore f(2) + f(-2) = 26 + 2$ $= 28$	$\frac{1}{2}$ $\frac{1}{2}$  1
	c)	Find $\frac{dy}{dx}$ if $y = \log x + \log_5 x + \log_5 5$	<b>02</b>
	Ans	$y = \log x + \log_5 x + \log_5 5$	

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1.	c)	$\therefore y = \log x + \frac{\log x}{\log 5} + \log_5 5$ $\therefore \frac{dy}{dx} = \frac{1}{x} + \frac{1}{x \log 5} + 0$ $\therefore \frac{dy}{dx} = \frac{1}{x} + \frac{1}{x \log 5}$	2
	d)	Evaluate $\int \sin^2 x \, dx$	02
	Ans	$\int \sin^2 x \, dx$ $= \frac{1}{2} \int 2 \sin^2 x \, dx$ $= \frac{1}{2} \int (1 - \cos 2x) \, dx$ $= \frac{1}{2} \left( x - \frac{\sin 2x}{2} \right) + c$	1 1
	e)	Evaluate $\int (x^a + a^x + a^a) \, dx$	02
Ans	$\int (x^a + a^x + a^a) \, dx$ $= \frac{x^{a+1}}{a+1} + \frac{a^x}{\log a} + a^a x + c$	2	
f)	Find the area under the curve $y = e^x$ bet <sup>n</sup> the ordinates $x = 0$ and $x = 1$		02
Ans	$\text{Area } A = \int_a^b y \, dx$ $= \int_0^1 e^x \, dx$ $= [e^x]_0^1$ $= e^1 - e^0$ $= e - 1$	1/2 1/2 1/2 1/2	

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1.	g)	An unbiased coin is tossed 5 times. Find the probability of getting three heads.	
	Ans	$n = 5, p = \frac{1}{2}, q = \frac{1}{2}, r = 3$ $\therefore P(r) = {}^n C_r p^r q^{n-r}$ $\therefore P(3) = {}^5 C_3 \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^{5-3}$ $\therefore P(3) = \frac{5}{16}$ or 0.3125	1 1
2.		Attempt any <b>THREE</b> of the following:	12
	a)	If $x^2 + y^2 = 4xy$ find $\frac{dy}{dx}$ at $(2, -1)$	04
	Ans	$x^2 + y^2 = 4xy$ $\therefore 2x + 2y \frac{dy}{dx} = 4 \left( x \frac{dy}{dx} + y \cdot 1 \right)$ $\therefore 2x + 2y \frac{dy}{dx} = 4x \frac{dy}{dx} + 4y$ $\therefore (2y - 4x) \frac{dy}{dx} = 4y - 2x$ $\therefore \frac{dy}{dx} = \frac{4y - 2x}{2y - 4x}$ $\therefore \frac{dy}{dx} = \frac{2y - x}{y - 2x}$ at $(2, -1)$ $\therefore \frac{dy}{dx} = \frac{2(-1) - 2}{-1 - 2(2)}$ $\therefore \frac{dy}{dx} = \frac{4}{5}$	2 1
	b)	If $x = a(1 + \cos \theta)$ , $y = a(1 - \cos \theta)$ find $\frac{dy}{dx}$	04
	Ans	$x = a(1 + \cos \theta)$ , $y = a(1 - \cos \theta)$	

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2.	b)	$\therefore \frac{dx}{d\theta} = -a \sin \theta$ , $\frac{dy}{d\theta} = a \sin \theta$	1+1
	Ans	$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{a \sin \theta}{-a \sin \theta}$ $\therefore \frac{dy}{dx} = -1$	1 1
	c)	A metal wire of 40 cm long is bent to form a rectangle. Find its dimensions when its area is maximum.	<b>04</b>
	Ans	$2x + 2y = 40$ $\therefore x + y = 20$ $\therefore y = 20 - x$ Area $A = xy$ $\therefore A = x(20 - x)$ $\therefore A = 20x - x^2$ $\therefore \frac{dA}{dx} = 20 - 2x$ $\therefore \frac{d^2A}{dx^2} = -2$ Consider $\frac{dA}{dx} = 0$ $20 - 2x = 0$ $\therefore x = 10$ at $x = 10$ $\therefore \frac{d^2A}{dx^2} = -2 < 0$ $\therefore$ Area is maximum at $x = 10$ $\therefore x = 10, y = 10$	1 1 1/2 1 1/2
	d)	A telegraph wire hangs in the form of a curve $y = a \cdot \log \sec \left( \frac{x}{a} \right)$ where 'a' is constant.  Show that the curvature at any point is $\frac{1}{a} \cdot \cos \left( \frac{x}{a} \right)$ .	<b>04</b>

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3.	a)	$y = x(2 - x)$ $\therefore y = 2x - x^2$ $\therefore \frac{dy}{dx} = 2 - 2x$ at (2,0) $\therefore \frac{dy}{dx} = 2 - 2(2)$ $\therefore \frac{dy}{dx} = -2$ $\therefore$ slope of tangent, $m = -2$ Equation of tangent at (2,0) is $y - 0 = -2(x - 2)$ $\therefore y = -2x + 4$ $\therefore 2x + y - 4 = 0$ $\therefore$ slope of normal, $m' = \frac{-1}{m} = \frac{1}{2}$ Equation of normal at (2,0) is $y - 0 = \frac{1}{2}(x - 2)$ $\therefore 2y = x - 2$ $\therefore x - 2y - 2 = 0$	<p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p> <p>1/2</p>
	b)	Find $\frac{dy}{dx}$ if $y = a^x + x^a + a^a + x^x$ Ans $y = a^x + x^a + a^a + x^x$ Let $u = x^x$ Taking log on both sides, $\therefore \log u = \log x^x$ $\therefore \log u = x \log x$ $\therefore \frac{1}{u} \frac{du}{dx} = x \frac{1}{x} + \log x \cdot 1$ $\therefore \frac{1}{u} \frac{du}{dx} = 1 + \log x$	<p>04</p> <p>1</p>

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3.	b)	$\therefore \frac{du}{dx} = u(1 + \log x)$ $\therefore \frac{du}{dx} = x^x(1 + \log x)$ $y = a^x + x^a + a^a + x^x$ $\therefore \frac{dy}{dx} = a^x \log a + ax^{a-1} + 0 + x^x(1 + \log x)$ $\therefore \frac{dy}{dx} = a^x \log a + ax^{a-1} + x^x(1 + \log x)$	1 2
	c)	<p>If <math>y = \tan^{-1}\left(\frac{5x}{1-6x^2}\right)</math> find <math>\frac{dy}{dx}</math></p> <p>Ans <math>y = \tan^{-1}\left(\frac{5x}{1-6x^2}\right)</math></p> $\therefore y = \tan^{-1}\left(\frac{3x+2x}{1-(3x)(2x)}\right)$ $\therefore y = \tan^{-1}(3x) + \tan^{-1}(2x)$ $\therefore \frac{dy}{dx} = \frac{1}{1+(3x)^2}(3) + \frac{1}{1+(2x)^2}(2)$ $\therefore \frac{dy}{dx} = \frac{3}{1+9x^2} + \frac{2}{1+4x^2}$	04 1 1 2
	d)	<p>Evaluate <math>\int \frac{(x-1)e^x}{x^2 \cdot \sin^2\left(\frac{e^x}{x}\right)} dx</math></p> <p>Ans <math>\int \frac{(x-1)e^x}{x^2 \cdot \sin^2\left(\frac{e^x}{x}\right)} dx</math></p> <p>Put <math>\frac{e^x}{x} = t</math></p> $\therefore \frac{xe^x - e^x \cdot 1}{x^2} dx = dt$	04 1

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3.	d)	$\therefore \frac{e^x(x-1)}{x^2} dx = dt$ $\int \frac{1}{\sin^2 t} dt$ $= \int \operatorname{cosec}^2 t dt$ $= -\cot t + c$ $= -\cot\left(\frac{e^x}{x}\right) + c$	<p>1</p> <p>1</p> <p>1</p>
4.		<p>Attempt any <b>THREE</b> of the following:</p> <p>a) Evaluate <math>\int \frac{1}{x+\sqrt{x}} dx</math></p> <p>Ans <math>\int \frac{1}{x+\sqrt{x}} dx</math></p> $= \int \frac{1}{\sqrt{x}(\sqrt{x}+1)} dx$ <p>Put <math>\sqrt{x}+1=t</math></p> $\therefore \frac{1}{2\sqrt{x}} dx = dt$ $\therefore \frac{1}{\sqrt{x}} dx = 2dt$ $= 2 \int \frac{1}{t} dt$ $= 2 \log t + c$ $= 2 \log(\sqrt{x}+1) + c$	<p>12</p> <p>04</p> <p>1</p> <p>1</p> <p>1</p>
	b)	<p>Evaluate <math>\int \frac{dx}{5+4\cos x}</math></p> <p>Ans <math>\int \frac{dx}{5+4\cos x}</math></p>	<p>04</p>

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4.	e) Ans	<p>Let <math>I = \int_0^5 \frac{\sqrt{9-x}}{\sqrt{9-x} + \sqrt{x+4}} dx</math> -----(1)</p> <p><math>I = \int_0^5 \frac{\sqrt{9-(5-x)}}{\sqrt{9-(5-x)} + \sqrt{5-x+4}} dx</math></p> <p><math>\therefore I = \int_0^5 \frac{\sqrt{9-5+x}}{\sqrt{\sqrt{9-5+x}} + \sqrt{9-x}} dx</math></p> <p><math>\therefore I = \int_0^5 \frac{\sqrt{4+x}}{\sqrt{\sqrt{4+x}} + \sqrt{9-x}} dx</math> -----(2)</p> <p>add (1) and (2)</p> <p><math>\therefore I + I = \int_0^5 \frac{\sqrt{9-x}}{\sqrt{9-x} + \sqrt{x+4}} dx + \int_0^5 \frac{\sqrt{4+x}}{\sqrt{\sqrt{4+x}} + \sqrt{9-x}} dx</math></p> <p><math>\therefore 2I = \int_0^5 \frac{\sqrt{9-x} + \sqrt{4+x}}{\sqrt{9-x} + \sqrt{x+4}} dx</math></p> <p><math>\therefore 2I = \int_0^5 1 dx</math></p> <p><math>\therefore 2I = [x]_0^5</math></p> <p><math>\therefore 2I = 5 - 0</math></p> <p><math>\therefore I = \frac{5}{2}</math></p>	<p>1</p> <p>1</p> <p>1/2</p> <p>1</p> <p>1/2</p>
5.	a) Ans	<p><b>Attempt any <u>TWO</u> of the following:</b></p> <p>Find the area bounded by curves <math>y^2 = x</math> and <math>x^2 = y</math></p> <p><math>y^2 = x</math> -----(1)</p> <p><math>x^2 = y</math></p> <p><math>\therefore \text{eq}^n. (1) \Rightarrow x^4 = x</math></p> <p><math>\therefore x^4 - x = 0</math></p> <p><math>\therefore x^3(x-1) = 0</math></p> <p><math>\therefore x = 0, 1</math></p> <p>Area <math>A = \int_a^b (y_1 - y_2) dx</math></p>	<p>12</p> <p>1</p>

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5.	a)	$\therefore A = \int_0^1 (\sqrt{x} - x^2) dx$ $\therefore A = \left( \frac{x^{\frac{3}{2}}}{\frac{3}{2}} - \frac{x^3}{3} \right)_0^1$ $\therefore A = \left( \frac{(1)^{\frac{3}{2}}}{\frac{3}{2}} - \frac{(1)^3}{3} \right) - 0$ $\therefore A = \left( \frac{2}{3} - \frac{1}{3} \right)$ $\therefore A = \frac{1}{3} \quad \text{or} \quad 0.333$	1  2  1  1
	b)	Attempt the following	<b>06</b>
	i)	Solve the differential equation $\frac{dy}{dx} + y \tan x = \cos^2 x$	<b>03</b>
	Ans	$\frac{dy}{dx} + y \tan x = \cos^2 x$ $\therefore \text{Comparing with } \frac{dy}{dx} + Py = Q$ $P = \tan x, \quad Q = \cos^2 x$ $\text{Integrating factor } IF = e^{\int \tan x dx} = e^{\log(\sec x)} = \sec x$ $\text{Solution is,}$ $y \cdot IF = \int Q \cdot IF dx + c$ $\therefore y \sec x = \int \cos^2 x \sec x dx$ $\therefore y \sec x = \int \cos^2 x \frac{1}{\cos x} dx$ $\therefore y \sec x = \int \cos x dx$ $\therefore y \sec x = \sin x + c$	1  1  1

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5.	b) ii)	<p>Find order and degree of the differential equation</p> $\frac{d^2y}{dx^2} = \sqrt[4]{y + \left(\frac{dy}{dx}\right)^2}$ <p>Ans</p> $\frac{d^2y}{dx^2} = \sqrt[4]{y + \left(\frac{dy}{dx}\right)^2}$ $\left(\frac{d^2y}{dx^2}\right)^4 = y + \left(\frac{dy}{dx}\right)^2$ <p>∴ Order = 2 Degree = 4</p> <hr/>	<p>1 1 1</p>

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5.	c)	<p>Acceleration of a moving particle at the end of 't' seconds from the start of its motion is <math>(5 - 2t) \text{ m/s}^2</math>. Find its velocity at the end of 3 seconds and distance travelled by it during that period, if its initial velocity is <math>4 \text{ m/s}</math>.</p> <p>Ans Acceleration = <math>5 - 2t</math></p> <p>i.e. <math>a = \frac{dv}{dt} = 5 - 2t</math></p> <p><math>\therefore \int dv = \int (5 - 2t) dt</math></p> <p><math>\therefore v = 5t - t^2 + c_1</math></p> <p>when <math>t = 0, v = 4 \therefore c_1 = 4</math></p> <p><math>\therefore v = 5t - t^2 + 4</math></p> <p>when <math>t = 3</math></p> <p><math>\therefore v = 5(3) - (3)^2 + 4 = 10 \text{ m/s}</math></p> <p><math>\therefore v = \frac{dx}{dt} = 5t - t^2 + 4</math></p> <p><math>\therefore dx = (5t - t^2 + 4) dt</math></p> <p><math>\therefore \int dx = \int (5t - t^2 + 4) dt</math></p> <p><math>\therefore x = \frac{5t^2}{2} - \frac{t^3}{3} + 4t + c_2</math></p> <p>at <math>t = 0, x = 0 \therefore c_2 = 0</math></p> <p><math>\therefore x = \frac{5t^2}{2} - \frac{t^3}{3} + 4t</math></p> <p>at <math>t = 3</math></p> <p><math>\therefore x = \frac{5(3)^2}{2} - \frac{(3)^3}{3} + 4(3) = 25.5 \text{ m}</math></p>	<p><b>06</b></p> <p>1/2</p> <p>1</p> <p>1/2</p> <p>1</p> <p>1/2</p> <p>1/2</p> <p>1</p>
6.		<p><b>Attempt any TWO of the following:</b></p> <p>a) Attempt the following</p> <p>i) The probability that a man aged 65 will live to 75 is 0.65. What is the probability that out of 10 men which are now 65, 7 will live to 75.</p> <p>Ans Given <math>p = 0.65, q = 1 - 0.65 = 0.35, n = 10, r = 7</math></p>	



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5.	a) i)	$\because p(r) = {}^n C_r (p)^r (q)^{n-r}$ $\therefore p(7) = {}^{10} C_7 (0.65)^7 (0.35)^{10-7}$ $\therefore p(7) = 0.2522$	2 1
	a) ii)	<p>The probability that a bomb dropped from a Plane will strike the target is <math>\frac{1}{5}</math>. If six bombs are dropped, find the probability that exactly two will strike the target.</p> <p>Ans Given</p> $p = \frac{1}{5} = 0.2, q = 1 - 0.2 = 0.8$ $n = 6, r = 2$ $\because p(r) = {}^n C_r (p)^r (q)^{n-r}$ $\therefore p(2) = {}^6 C_2 (0.2)^2 (0.8)^{6-2}$ $\therefore p(2) = 0.2458$	03 2 1
	b)	<p>If 2% of the electric bulbs manufactured by company are defective, find the probability that in a sample of 100 bulbs.</p> <p>(i) 3 bulbs are defective,</p> <p>(ii) At the most two bulbs will be defective. (<math>e^{-2} = 0.1353</math>)</p> <p>Ans <math>p = 2\% = 0.02, n = 100</math></p> $\therefore \text{mean } m = np$ $\therefore m = 100 \times 0.02 = 2$ <p>Poisson's distribution is,</p> $P(r) = \frac{e^{-m} \cdot m^r}{r!}$ <p>(i) 3 bulbs are defective <math>\therefore r = 3</math></p> $\therefore P(3) = \frac{e^{-2} (2)^3}{3!}$ $\therefore P(3) = 0.1804$ <p>(ii) At the most two bulbs will be defective <math>\therefore r = 0, 1, 2</math></p>	06 1 1 1

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6.	c)	$\therefore p(\text{more than } 2150) = 0.0336$ $\therefore \text{No. of students} = N \cdot p = 2000 \times 0.0336$ $= 67.2 \approx 67$	1  1/2
<p><b><u>Important Note</u></b></p> <p><i>In the solution of the question paper, wherever possible all the possible alternative methods of solution are given for the sake of convenience. Still student may follow a method other than the given herein. In such case, first see whether the method falls within the scope of the curriculum, and then only give appropriate marks in accordance with the scheme of marking.</i></p>			

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